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Compiler Construction

Lecture 5: Introduction to Parsing

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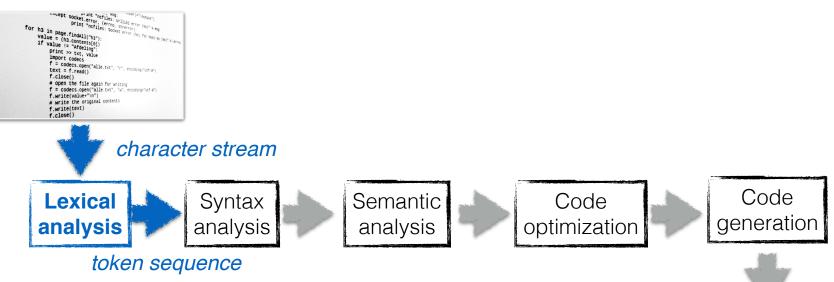
Overview

- Compiler structure revisited
 - Interaction of scanner and parser
- Context-free languages
- Ambiguity of grammars
- BNF grammars
- Language classes and Chomsky hierarchy



Stages of a compiler ⁽¹⁾

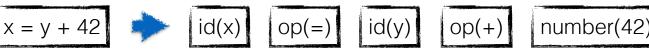
Source code



Lexical analysis (scanning):

- Split source code into *lexical units*

- Recognize tokens (using regular expressions/automata) machine-level program
- Token: character sequence relevant to source language grammar



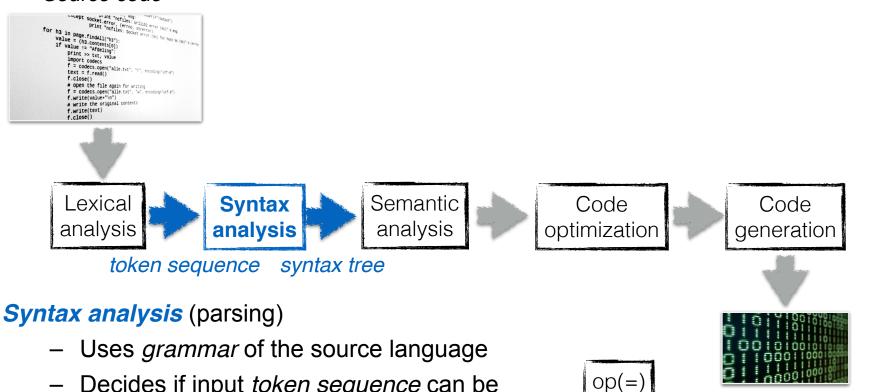
character stream

token sequence

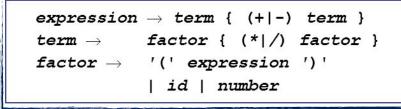
Compiler Construction 05: Introduction to Parsing

Stages of a compiler ⁽²⁾

Source code



 Decides if input *token sequence* can be derived from the grammar



id(y) number(42)

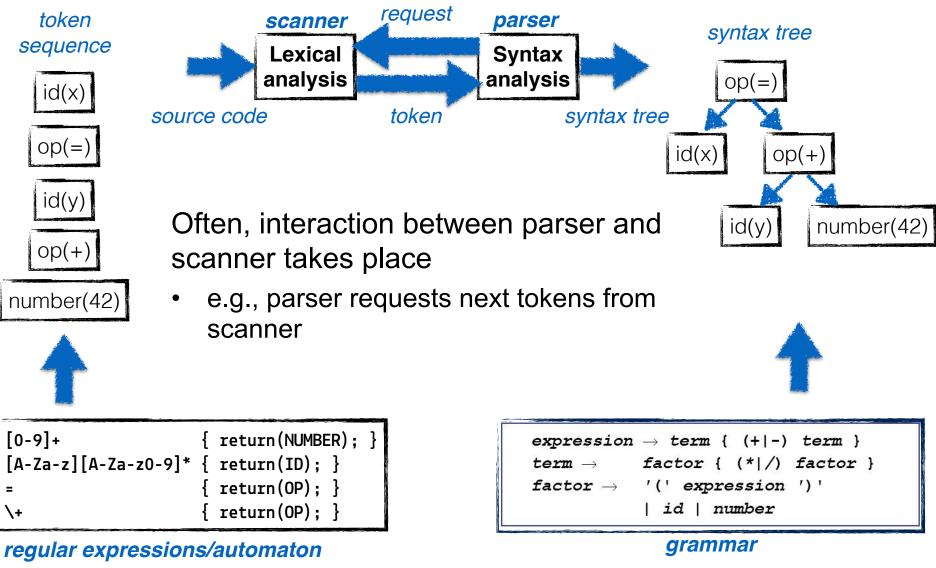
op(+)

machine-level program



id(x)

Interaction of scanner and parser



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Parsing

- Parsing is the second stage of the compiler's front end
 - it works with program as transformed by the scanner
 - it sees a stream of words
 - each word is annotated with a syntactic category



- Parser derives a syntactic structure for the program
 - it fits the words into a grammatical model of the source programming language
- Two possible outcomes:
 - Input is valid program: builds a concrete model of the program for use by the later phases of compilation
 - X input is not a valid program: report problem and diagnosis

Definition of parsing



- Task of the parser:
 - determining if the program being compiled is a valid sentence in the syntactic model of the programming language
- A bit more formal:
 - the syntactic model is expressed as *formal grammar G*
 - some string of words s is in the language defined by G we say that G derives s
 - for a stream of words s and a grammar G, the parser tries to build a constructive proof that s can be derived in G

— this is called parsing

- It's not as bad as it sounds...
 - we let the computer do (most of) the work!

Specifying language syntax

- We need...
 - a formal mechanism for specifying the syntax of the source language (grammar)
 - a systematic method of determining membership in this formally specified language (parsing)
- Let's make our lives a bit easier
 - we restrict the form of the source language to a set of languages called *context-free languages*
 - typical parsers can efficiently answer the membership question for those
- Many different parsing algorithms exist, we will look at
 - top-down parsing: recursive descent and LL(1) parsers
 - **bottom-up parsing:** LR(1) parsers

Parsing approaches in general

- **Top-down parsing:** recursive descent and LL(1) parsers
 - Top-down parsers try to match the input stream against the productions of the grammar by predicting the next word (at each point)
 - For a limited class of grammars, such prediction can be both accurate and efficient
- **Bottom-up parsing:** LR(1) parsers
 - Bottom-up parsers work from low-level detail—the actual sequence of words—and accumulate context until the derivation is apparent
 - Again, there exists a restricted class of grammars for which we can generate efficient bottom-up parsers
- In practice, these restricted sets of grammars are large enough to encompass most features of interest in programming languages

Expressing syntax

- We already know a way to express syntax: regular expressions
- Why are regexps not suitable for describing language syntax?

Example: recognizing algebraic expressions over variables and the operators +, -, ×, ÷

variable = [a...z]([a...z] | [0...9])*
expression = [a...z]([a...z] | [0...9])* ((+|-|×|÷) [a...z]([a...z] | [0...9])*)*

- This regexp matches e.g. "a+b×c" and "dee+daa×doo"
- However, there is no way to express *operator precedence*
 - should + or × be executed first in "a+b×c"?
 - standard rule from algebra suggests:
 "× and ÷ have precedence over + and -"

Expressing syntax: regexps?

variable = [a...z] ([a...z] | [0...9])* expression = [a...z] ([a...z] | [0...9])* ((+|-|×|÷) [a...z] ([a...z] | [0...9])*)*

- There is no way to express *operator precedence*
 - to enforce evaluation order, algebraic notation uses parentheses
 Literal parentheses are printer
 Under parentheses in response in this is not and enclosed in "": "("
- Adding parentheses in regexps is tricky...
 - an expression can start with a "(", so we need the option for an initial "(". Similarly, we need the option for a final ")":

$("("|\varepsilon) [a_{m}z]([a_{m}z]|[0_{m}9])* ((+|-|\times|\div) [a_{m}z] ([a_{m}z]|[0_{m}9])*)* (")"|\varepsilon)$

 This regexp can produce an expression enclosed in parentheses, but *not one with internal parentheses* to denote precedence



Svntax

Expressing syntax: regexps?

$("("|\varepsilon) [a_{m}z]([a_{m}z]|[0_{m}9])* ((+|-|\times|\div) [a_{m}z] ([a_{m}z]|[0_{m}9])*)* (")"|\varepsilon)$

- This regexp can produce an expression enclosed in parentheses, but *not* one with internal parentheses to denote precedence
- Internal instances of "(" all occur before a variable
 - similarly, the internal instances of ")" all occur after a variable
 - so let's move the closing parenthesis inside the final *:

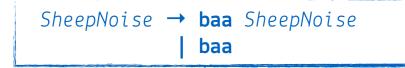
$("("|\epsilon) [a...z]([a...z]|[0...9])* ((+|-|×|÷) [a...z] ([a...z]|[0...9])* (")"|\epsilon))*$

- This regexp matches both "a+b×c" and "(a+b)×c."
 - it will match *any* correctly parenthesized expression over variables and the four operators in the regexp
- Unfortunately, it also *matches many syntactically incorrect expressions*
 - such as "a+(b×c" and "a+b)×c)."
- We cannot write a regexp matching all expressions with balanced parentheses: "DFAs cannot count"



Context-Free Grammars

- We need a more powerful notation than regular expressions
 - ...that still leads to efficient recognizers
- Traditional solution: use a *context-free grammar* (CFG)
 - grammar G: set of rules that describe how to form sentences
 - *language* L(G) defined by G: collection of sentences that can be derived from G
- Example: consider the following grammar SN





• each line describes a *rule* or *production* of the grammar

•

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Context-Free Grammars



SheepNoise → **baa** SheepNoise baa

- The first rule SheepNoise \rightarrow **baa** SheepNoise reads: "SheepNoise can derive the word baa followed by more SheepNoise"
- SheepNoise is a syntactic variable representing the set of strings that can be derived from the grammar written in italics
 - We call these syntactic variables "nonterminal symbols" NT Each word in the language defined by the grammar (baa) is a "terminal symbol" written in **bold** letters "|" can be read as "OR":
- The second rule reads: "SheepNoise can also () derive the string baa"
 - The "|"-notation is a shorthand to avoid writing two separate rules:

SheepNoise → **baa** SheepNoise SheepNoise → baa

the parser can choose either

the first or the second rule

Grammars and languages



SheepNoise → baa SheepNoise | baa

- Can we figure out which sentences can be derived from a grammar G?
 - i.e., what are valid sentences in the language *L*(G)?
- First, identify the goal symbol or start symbol of G
 - represents the set of all strings in L(G)
 - thus, it cannot be one of the words in the language
- Instead, it must be one of the nonterminal symbols introduced to add structure and abstraction to the language
 - Since our grammar SN has only one nonterminal, SheepNoise must be the start symbol

Grammars and languages





- Deriving a sentence:
 - start with a prototype string that contains just the start symbol, SheepNoise
 - pick a nonterminal symbol, α , in the prototype string
 - choose a grammar rule, $\alpha \rightarrow \beta$
 - and rewrite (replace) α with β
- Repeat until the prototype string contains no more nonterminals
 - the string then consists entirely of words (terminal symbols)
 - \Rightarrow it is a sentence in the language
 - every version of the prototype string that can be derived is called a *sentential form*

Grammars and languages





• Examples:

Rule	Sentential form		
	SheepNoise		
2	baa		

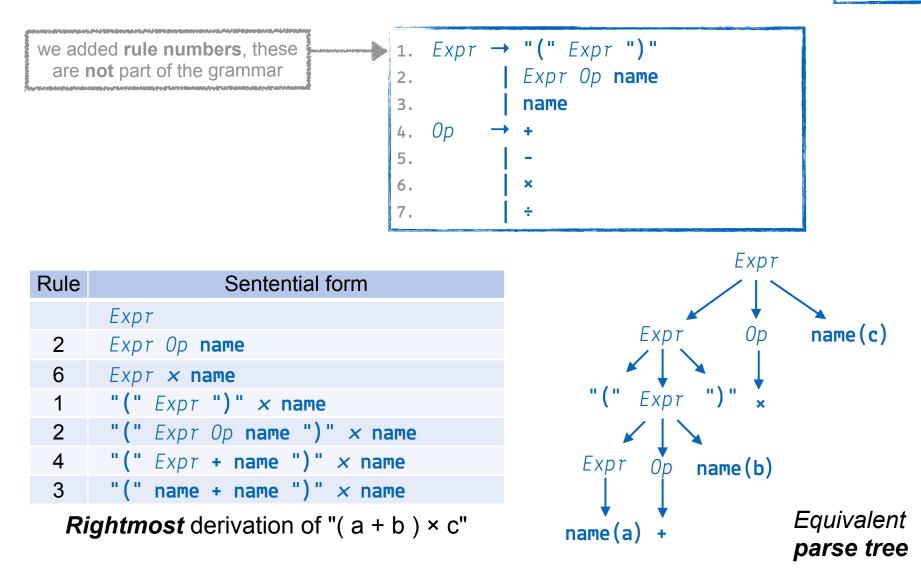
Rewrite with rule 2

Rule	Sentential form			
	SheepNoise			
1	baa SheepNoise			
2	baa baa			

Rewrite with rule 1, then rule 2

- Rule 1 lengthens the string while rule 2 eliminates the NT SheepNoise
- The string can never contain more than one instance of *SheepNoise*
- All valid strings are derived by >= 0 applications of rule 1, followed by rule 2
- Applying rule 1 *k* times followed by rule 2 generates a string with *k*+1 baas.

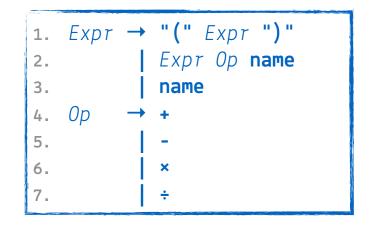
A more useful example...

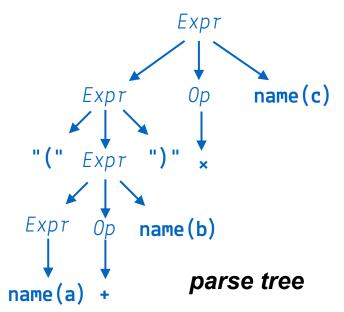


Syntax

A more useful example...

- This simple context-free grammar for expressions cannot generate a sentence with unbalanced or improperly nested parentheses
 - Only rule 1 can generate an open parenthesis; it also generates the matching close parenthesis
- Thus, it cannot generate strings such as "a+(b×c" or "a+b)×c)"
 - a parser built from the grammar will not accept such strings
- Context-free grammars allow to specify constructs that regexps do not







Order of derivations

Expr → "(" Expr ")" 1. *Rightmost*: Expr Op name 2. rewrite, at each step, the rightmost nonterminal 3. name Rule Sentential form 0p 4. Ехрт 5. Expr Op name 6. Expr x name 7. "(" Expr ")" × name "(" Expr Op name ")" × name Expr "(" Expr + name ")" × name "(" name + name ")" × name Leftmost: rewrite, at each step, the leftmost nonterminal Expr name(c) 0p Sentential form Rule Expr Expr Op name 2 "(" Expr ")" Op name "(" Expr Op name ")" Op name Expr 00 name(b) "(" name Op name ")" Op name parse tree "(" name + name ")" Op name identical for both! name(a) "(" name + name ")" × name



2

6

1

2

4

3

1

2

3

4

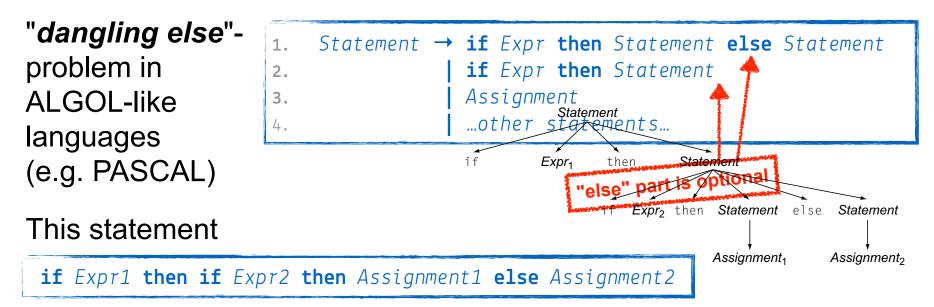
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Syntax

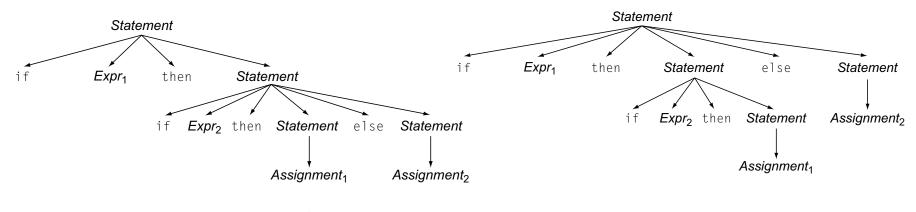
Ambiguity of grammars

- For the compiler, it is important that each sentence in the language defined by a context-free grammar has a *unique* rightmost (or leftmost) *derivation*
- A grammar in which multiple rightmost (or leftmost) derivations exist for a sentence is called an *ambiguous grammar*
 - it can produce multiple derivations and multiple parse trees
- Multiple parse trees imply *multiple possible meanings for a* single program!

Ambiguity of grammars: example



has two distinct rightmost derivations with different behaviors:



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Syntax

Removing ambiguity



We can modify the grammar to include a rule that determined which **if** controls an **else**:

1.	Statement	→	if Expr then Statement
2.			<pre>if Expr then WithElse else Statement</pre>
3.			Assignment
4.	WithElse	\rightarrow	<pre>if Expr then WithElse else WithElse</pre>
5.			Assignment

This solution restricts the set of statements that can occur in the **then** part of an **if-then-else** construct

- It accepts the same set of sentences as the original grammar
- but ensures that each else has an unambiguous match to a specific if



Removing ambiguity: example

The modified grammar has only one rightmost derivation for the example

1.	Statement	→	if Expr then Statemen
2.			<pre>if Expr then WithElse else Statement</pre>
3.			Assignment
4.	WithElse	→	<pre>if Expr then WithElse else WithElse</pre>
5.			Assignment

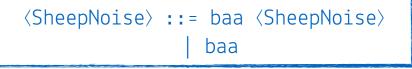
if Expr1 then if Expr2 then Assignment1 else Assignment2

Rule	Sentential form		
	Statement		
1	if Expr then Statement		
2	<pre>if Expr then if Expr then WithElse else Statement</pre>		
3	<pre>if Expr then if Expr then WithElse else Assignment</pre>		
5	if Expr then if Expr then Assignment else Assignment		

Syntax

Addendum: Backus-Naur-Form

- Syntax analysis
- The traditional notation to represent a context-free grammar is called *Backus-Naur form* (BNF) [1]
 - BNF denotes nonterminal symbols by wrapping them in angle brackets, like (SheepNoise)
 - Terminal symbols are <u>underlined</u>.
 - The symbol ::= means "derives," and the symbol | means "also derives"
- In BNF, the sheep noise grammar becomes:



• This is equivalent to our grammar SN

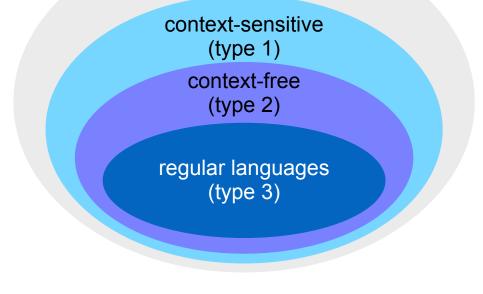
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...and was easier to typeset in the 1950's

Addendum: Types of languages

- Noam Chomsky (*1928): American linguist, philosopher, cognitive scientist, historian, social critic, and political activist
- The **Chomsky hierarchy** is a containment hierarchy of classes of formal grammars [2]
- Defines four types (0–3) of languages with increasing complexity from regular languages to recursively enumerable
- Accordingly, recognizing the language requires a successively more complex method



recursively enumerable (type 0)



Svntax

References

 P. Naur (Ed.), J.W. Backus, F.L. Bauer, J. Green, C. Katz, J. McCarthy, et al.: Revised report on the algorithmic language Algol 60, Commun. ACM 6 (1) (1963) 1–17

[2] Noam Chomsky, Marcel P. Schützenberger: The algebraic theory of context free languages, In Braffort, P.; Hirschberg, D. (eds.). Computer Programming and Formal Languages Amsterdam: North Holland. pp. 118–161, 1963

