

Compiler Construction

Lecture 19–1: Data flow analyses – Overview

Week of 2020-03-16

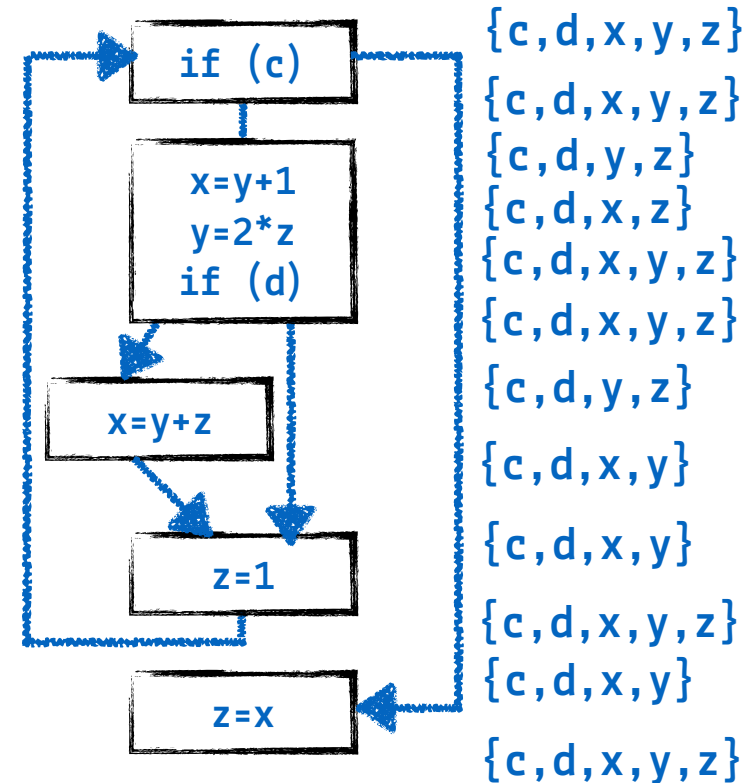
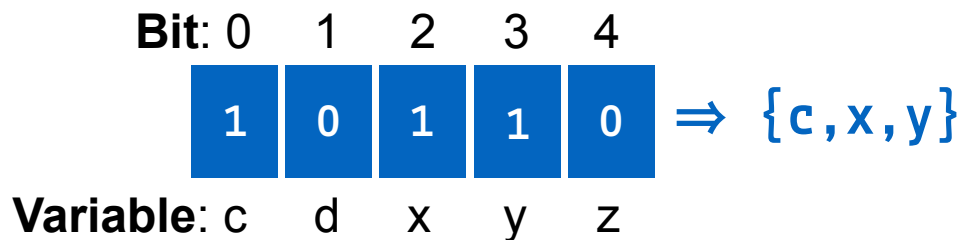
Michael Engel

Classical bit-vector data-flow analyses

- Origins of data flow analysis were the so-called “bit vector” data flow frameworks [1]
 - called “bit vector” since data flow and additional information are represented using bit vectors
 - the analysis can be performed using bit vector operations alone
- There are forms of data flow which require additional operations for performing analyses
 - the data flow information itself is still represented using bit vectors
 - we make this notion more precise later with the help of the examples presented here

Bit vectors as set representations

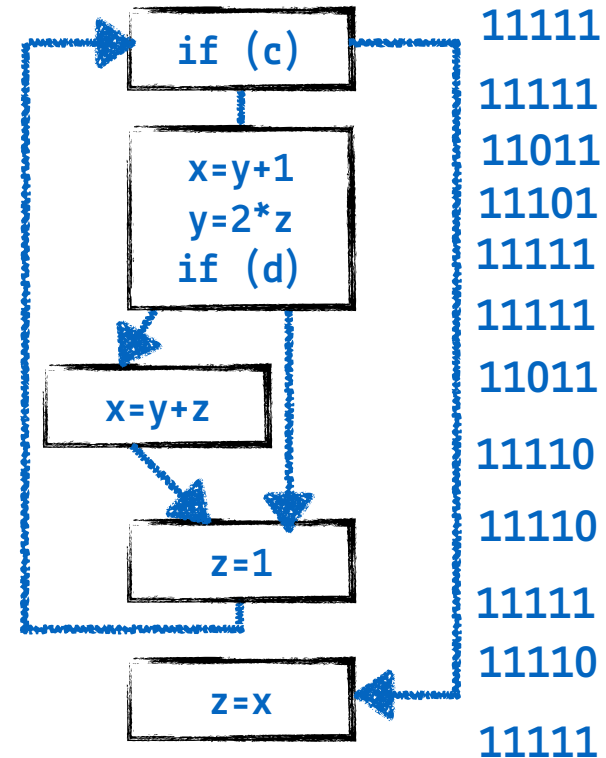
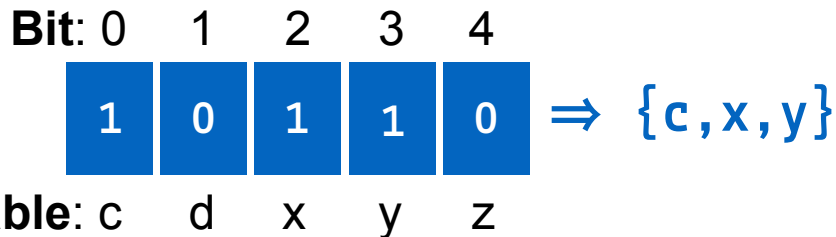
- Using bit vectors enables an **efficient** implementation of sets
- Example: set with 32 elements
 - The presence or absence of each element is represented by a specific bit set to 1 or 0, respectively
- Representation of variables **c,d,x,y,z** as 5 bit set:



Bit vectors as set representations

- We can use bit vectors to represent the sets of **live variables** at the program points of the example in lecture 17

efficient as long as the number of elements fits in a machine word



Set operations on bit vectors

- Typical set operations can now be implemented using boolean logic operators
- Example: **union** (join) of two sets (\cup) using **OR**:

Variable:	c	d	x	y	z	
	1	0	1	1	0	$\Rightarrow \{c, x, y\}$
OR	0	0	1	0	1	$\Rightarrow \{x, z\}$
<hr/>						
	1	0	1	1	1	$\Rightarrow \{c, x, y, z\} = \{c, x, y\} \cup \{x, z\}$

- The set property that each element may only occur once in a set is guaranteed by mapping set elements to bits

Set operations on bit vectors

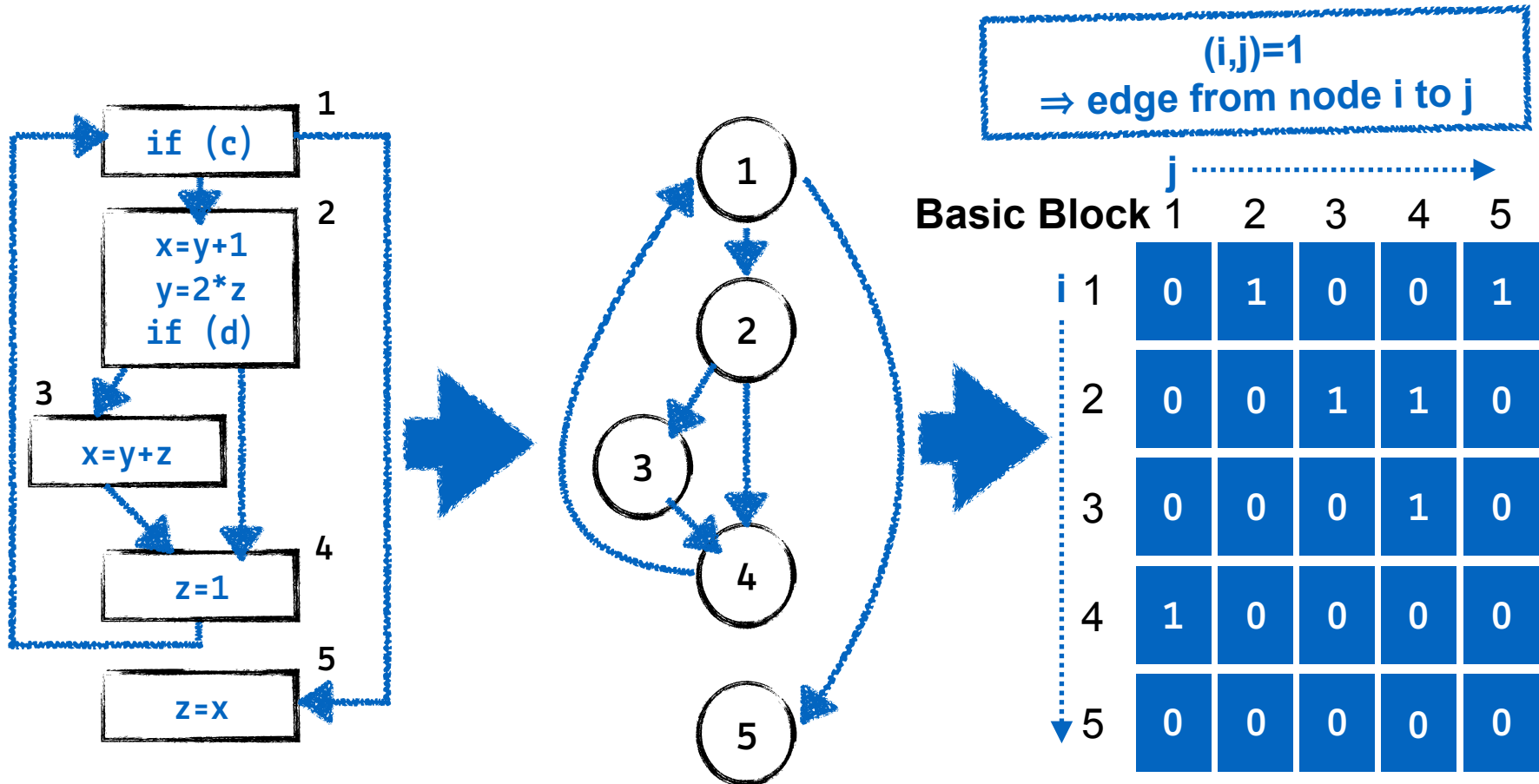
- Typical set operations can now be implemented using boolean logic operators
- Example: **intersection** (meet) of two sets (\cap) using **AND**:

Variable:	c	d	x	y	z	
	1	0	1	1	0	$\Rightarrow \{c, x, y\}$
AND	1	0	0	1	1	$\Rightarrow \{c, y, z\}$
<hr/>						
	1	0	0	1	0	$\Rightarrow \{c, y\} = \{c, x, y\} \cap \{c, y, z\}$

- Set complement can be implemented using **XOR**

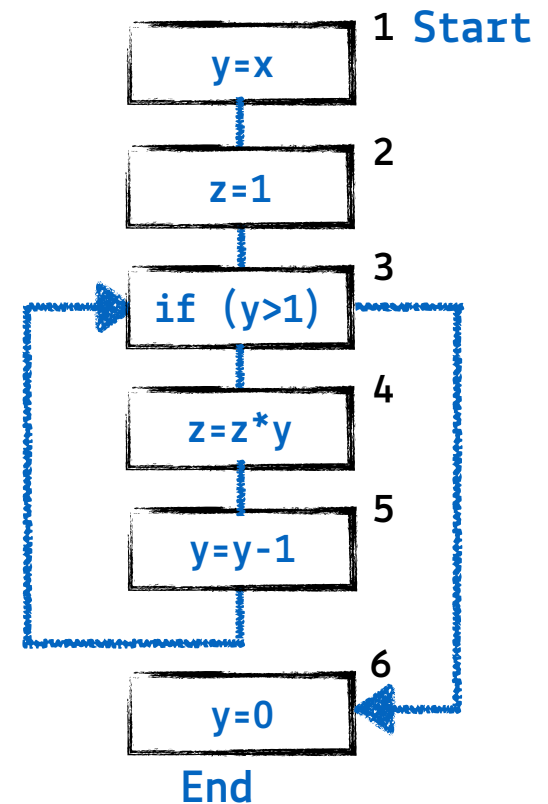
Bit vectors to represent graphs

- We can also use bit vectors to represent graphs (e.g. CFG)
- Bit vectors can represent a graph's *adjacency matrix*



Properties of CFGs

- Edges in CFGs denote **predecessor** and **successor** relationships
- For an edge $n1 \rightarrow n2$:
 - $n1$ is a **predecessor** of $n2$ ($n1 = \text{pred}(n2)$)
 - $n2$ is a **successor** of $n1$ ($n2 = \text{succ}(n1)$)
- CFG has two distinguished unique nodes:
 - **Start** which has no predecessor
 - **End** which has no successor
- Every basic block n is reachable from the **Start** block and the **End** block is reachable from n



Overview of data-flow analyses

- Data flow analysis views computation of data through expressions and transition of data through assignments to variables
- Properties of programs are defined in terms of properties of program entities such as expressions, variables, and definitions appearing in a program
 - we restrict expressions to primitive expressions involving a single operator
 - variables are restricted to scalar variables and definitions are restricted to assignments made to scalar variables
(let's keep it moderately simple...)

General approach

- For a given program entity such as an expression, data flow analysis of a program involves the following two steps
 - (a) discovering the effect of individual statements on the expression, and
 - (b) relating these effects across statements in the program
- For reasons of efficiency, both steps are often carried over a basic block instead of a single statement
- Step (a) is called **local** data flow analysis and is performed for a basic block only once
- Step (b) constitutes **global** data flow analysis and may require repeated traversals over basic blocks in a CFG

*"global" here means:
inside a single procedure!*

Discovering local data flow information

- The modelling of the effect of a statement varies between different analyses
- However, there is a common pattern of generation of data flow information or invalidation of data flow information

Entity	Operations	
Variable x	Reading the value of x (<i>use</i>)	Modifying the value of x
Expression e	Computing e	Modifying an operand of e
Definition $d_i : x = e$	Occurrence of d_i	Any definition of x

Entities and operations

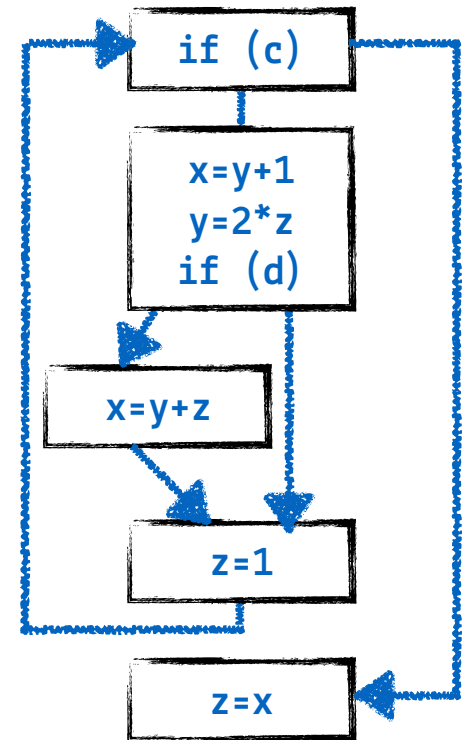
- A **variable** may be used or an **expression** may be computed
 - (a) in the right hand side of an assignment statement,
 - (b) in a condition for altering the control flow,
 - (c) as an actual parameter in a function call, or
 - (d) as a return value from a function
- All other operations involve an **assignment** statement to a relevant variable

- Note that **reading** a value of a variable **from input** can be safely considered as an assignment statement assigning an unknown value to the variable

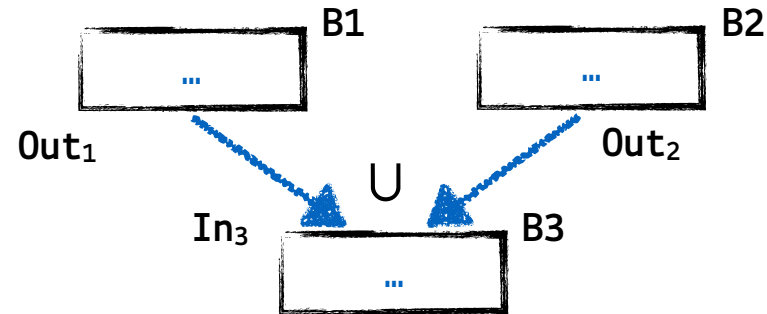
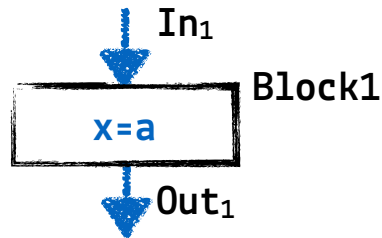
Entity	Operations	
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Relationship of CFG information

- The relationship between local and global data flow information for a block and between global data flow information across different blocks is captured by **data flow equations**
 - this is a system of linear simultaneous equations
- In general, these equations have multiple solutions



Data flow equations



- In forward flow analysis, the exit state of a basic block ***b*** is a function (***data flow equation***) of the block's entry state: $Out_b = trans_b(In_b)$
 - composition of the effects of the statements in the block
 - $trans_b$ is the ***transition function*** of block ***b***
- The entry state of a basic block is a function (***data flow equation***) of the exit states of its predecessors: $In_b = join_{p \in pred(b)}(Out_p)$
 - The join operation $join_{p \in pred(n)}$ combines the exit states of all predecessors ***p*** of ***b***, yielding the entry state of ***b***

Data-flow analysis directions

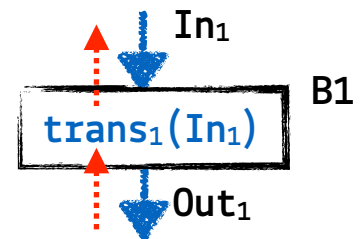
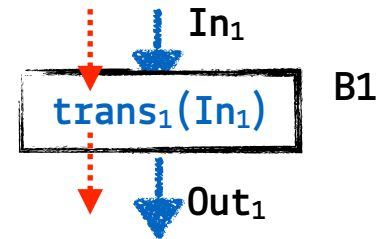
Each type of data-flow analysis has a **specific transfer function and join operation**

Forward analyses traverse the CFG **along** the direction of the control flow

- e.g. reaching definitions, available expressions

Backward analyses traverse the CFG **against** the direction of the control flow

- e.g. live variables analysis, very busy expressions
- Here, the transfer function is applied to the exit state yielding the entry state
 - the join operation works on the entry states of the successors to yield the exit state



Bit vector analysis: Gen and Kill sets

Bit vector dataflow analyses works on *sets of facts*

- these sets can be represented efficiently as bit vectors
- Join and transfer functions are implemented as logical bitwise ops
 - join is typically \cup or \cap , implemented by logical or / logical and
 - transfer functions can be decomposed into **Gen** and **Kill** sets
- **Gen**: points in the graph where a fact you care about becomes *true*
 - **Gen_b** describes data flow info. generated within block **b**
- **Kill**: points in the graph where a fact you care about becomes *false*
 - **Kill_b** describes data flow inf. which becomes invalid in block **b**
- **Gen_b** and **Kill_b** points thus depend on the facts you care about

Example: gen and kill sets

- **Example:** in *live-variable analysis*, the **join** operation is **union**
- **Kill set:** **variables that are written** in a block
- **Gen set:** **variables that are read without being written first**
- The related data-flow equations are thus:

$$Out_b = \bigcup_{s \in succ(b)} In_s \qquad In_b = (Out_b - Kill_b) \cup Gen_b$$

- In logical operations:

```
out(b) = 0           // empty set
for s in succ(b) {
    out(b) = out(b) or in(s)
}
in(b) = (out(b) and not kill(b))
        or gen(b)
```

References

- [1] Uday P. Khedker, Amitabha Sanyal, Bageshri Karkare. Data Flow Analysis: Theory and Practice. CRC Press, 2009 (Chapter 2, Classical Bit Vector Data Flow Analysis)
- [2] Flemming Nielson, Hanne Riis Nielson, Chris Hankin. Principles of Program Analysis. Springer, 2nd edition, 2005 (Chapter 2, Data Flow Analysis)
- [3] Robert Morgan. Building an Optimizing Compiler. Digital Press, 1998 (Chapter 4.12, Global Available Temporary Information)
- [4] Gary Kildall. A Unified Approach to Global Program Optimization. Proceedings of the 1st ACM Symposium on Principles of Programming Languages (POPL), 1973