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Compiler Construction

Lecture 17: Optimizations in detail

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Overview

- Optimizations
 - Control-flow graphs
 - Liveness of variables



Optimization

- We wish to apply various program transformations to improve its non-functional properties without changing its meaning
- Transformations can apply either at IR or lower levels
- Optimizations have to be safe
 - the optimized program must give the same results as the un-optimized program for every possible execution
- We need some structured approaches to ensure this...

The meaning of programs

- Information required for performing optimizations often is not explicitly contained in the source code
 - So we have to extract information
- Consider the following code:

• Are all these statements necessary?

Program meaning is implicit

• Some of the statements are *dead code*

X	=	y +	1;	←	This assignment of x
у	=	2 *	z;	←	is not used in any intermediate statement
х	=	y +	Ζ;	←	…until x is assigned again here
Z	=	1;		←	This assignment of z
z	=	Х;		←	is immediately overwritten

• Knowing this, we can construct a shorter identical program



- · Control flow is linear here, so the dead state is obvious
- It becomes harder to tell when control flow is involved

Conditions complicate everything

• If we add some control flow

x = y + 1; ← is this statement still dead? y = 2 * z; x = y + z; z = 1; ← what about that one? z = x;

• The first assignment to x may or may not be used again:

```
x = y + 1; ← x is reused in a loop here
y = 2 * z;
if (c) { x = y + z; }
z = 1; ← This still makes no difference
z = x;
```

• This assignment becomes relevant when the value of c is false

Loops complicate even more...

• If we insert a loop...

```
while (d) {
    x = y + 1; ← is this statement still dead?
    y = 2 * z;
    if (c) { x = y + z; }
    z = 1; ← is this statement still dead?
}
z = x;
```

• ...neither statement can be omitted!





Low-level code makes it worse...

 Control flow is more obvious from source code syntax than from its translation into jumps and labels:





What do we need?

- Methods to compute information that are
 - implicit in the program
 - static (so that it can be found at compile time)
 - valid for every possible dynamic situation (at runtime)
- A data structure that can represent every possible control flow
 - Different branches taken (conditionals)
 - Branches taken different numbers of times (loops)
- Problem is similar to that of NFA:
 "What are all the possible paths I can take from here?"

Control Flow Graphs (CFGs)

- Program control flow can be captured in a directed graph, where statements make nodes and their sequencing follows the arcs
- Movement of data can be inferred by traversing a structure like this
 - By far the most common approach in present compilers (It is also possible to graph data movement and infer control, but let's stick to the control flow view)
- Multiple paths emerge since nodes can have multiple incoming/ outgoing arcs

Linear code sequences

• Rather simple...

a = 1; b = 2; c = a + b;



• but remember that there are separate statements inside...







Branches end basic blocks

• This code needs multiple basic blocks:







Multiple paths

- Every possible execution is encoded in the CFG
- Each path corresponds to a run of the program





Choose your path...

When **c** is **true**:

When **c** is **false**:





Infeasible executions

Some paths may not correspond to any possible run:



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Infeasible executions

 \Rightarrow This path is *infeasible*, even though it is part of the CFG!



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Interpretation of arcs

- Without pruning infeasible paths (which may require run-time information), the analysis will remain conservative/safe as long as every actual path is also represented
- Outgoing arcs mean that their destination may be a successor to a basic block
- Incoming arcs mean that any of the source blocks *may be* a predecessor to a basic block







Recursive CFG construction

• At high level, CFGs can be built by a syntax directed scheme

Similar to our translation to TAC

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Recursive CFG construction: if/while

CFG(if(E) S) =

CFG(while (E) S) =







• We are analyzing statements recursively to refine our CFG:

S1	
 *	
S2	



• We are analyzing statements recursively to refine our CFG:





• We are analyzing statements recursively to refine our CFG:



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• We are analyzing statements recursively to refine our CFG:



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Efficiency

• Empty blocks and sequences can be pruned after or during construction of the CFG





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Efficiency

- These graphs grow large
 - It's good to have as few basic blocks as possible
 - They should be as large as possible
- Merge linear subgraphs if
 - B2 is a successor of B1
 - B1 has one outgoing edge
 - B2 has one incoming edge
 - $B1 \rightarrow B2$ should be a block
- Remove empty blocks

At low-level IR

- Split the operation sequence at labels and jumps
 - Labels can have incoming control flow
 - Jumps have outgoing control flow



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At low-level IR

- Conditional jump = 2 successors
- Unconditional jump = 1 successor



The outcome is the same

• Both procedures give us the equivalent program logic:







Live variables and the CFG

- The purpose of using the CFG is to statically extract information about the program at compile time
- Reasoning about the run-time values of variables and expressions in every possible execution enables optimizations
- We can illustrate this by finding *live variables*



Liveness

- A live variable is one which holds a value that may still be used at a later point
- Conversely, a dead variable is guaranteed to see no further use (until its next assignment)
- This means we're searching for ranges of instructions in the program where variables hold values that matter to the execution
- In order to find ranges of instructions, we need to define program points the ranges can span across



Program points

- As we want to capture how state is changed through an instruction, we need to talk about the state before and the state after, and describe the difference
- Hence, there is one program point before and one after each instruction



- For basic blocks, these are the points
 - after the predecessor(s)
 - before the successor(s)

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Program points in our previous ex.

• We mark the before and after points with dashed lines here:





Two things to consider

- How does an instruction affect the state at the points immediately before and after it?
 - In other words, what is the effect of an instruction?
- How does state propagate between program points?
 - In other words, what is the effect of control flow?
- If we can tell which variables are life at one point, we can compute which ones are live by its neighbors

Which instructions affect liveness?

 If a variable is used in an expression, it must be kept at the preceding program point:



• If a variable is **defined** in an expression, **it was dead** at the preceding program point:

a will not be used again here, it is overwritten in the following statement
a = b + 1



Doing it systematically

- For an instruction I, define two sets of variables
 - in[I] = set of live variables at point before I
 - out[I] = set of live variables at point after I
- This extends naturally to basic blocks
 - in[B] = set of live variables at point before B
 - **out[B]** = set of live variables at point after **B**
- ...so if **I1** and **I2** are the first and last instructions in **B**,
 - in[B] = in[I1]
 - out[B] = out[I2]

Before & after vs. instructions

- All variables used by an instruction must be live before it can use them
- Variables defined by an instruction are not live at the last point before the instruction

```
• So,
    live before = live after - defined vars + used vars
    or
    in[I] = out[I] - def(I) + use(I)
```



Before & after vs. control flow

- All variables used along the path of any successor must be live after the predecessor
 - You never know which path will be taken, one of them might need it
- Where control flows split,

live after = live before successor #1 + live before successor #2 + ...

or

```
out[I] = in[I1] + in[I2]
where I1, I2 are successors of I
```

Liveness flows backwards

- We define the in-sets in terms of the out-sets
- This means we need out-sets to start our analysis
- In the name of safety, assume that every variable is live until it has been determined otherwise
- This results in a final out-state to start working from, so that we can *examine the CFG in reverse*



Start at the end...

• Conservative assumption: everything is live at the end





The last statement defines z



• Its predecessor doesn't define anything



• Predecessor defines z, but it wasn't live anyway







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 Predecessor of two successors (control flow): must assume *union* of the live variables of each successor



• Definition of y





• Use of y, definition of z





End of iteration 1

- We've covered all points, but *something* changed
 - Repeat from the start... if (c) x=y+1 y=2*zif (d) x=y+z (c,d,x,y) (c,d,x,z) (c,d,x,z) (c,d,x,z) (c,d,x,y) (c,d,x,y)(c,d,x,y)





• The *union* of the two successors here is different



• Propagate it to the predecessor





• ...and again, until we've been through all nodes... (then repeat, because something changed)



• Nothing changes, we have reached a *fixed point*



Between the lines

- Every instruction implies a constraint equation
 - Live before = live after what it defines + what it uses
- Everywhere control flows join, there is another constraint equation
 - Live after = sum of what's live at all successors
- The framework for data flow analysis simply uses different instances of this pattern
 - Different constraint equations capture different information
 - Different split/join behavior follows from the type of information
 - May work forward or backward (liveness propagates backwards)
- We'll look at a handful of instances next week



What's next?

• Optimizations in detail: data-flow analyses

References

[1] Frances E. Allen. 1970.
 Control flow analysis. SIGPLAN Not. 5, 7 (July 1970), 1–19.
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