## **DTTNU** | Norwegian University of Science and Technology

#### **Compiler Construction**

Lecture 8: LR-parsing 2020-01-31 Michael Engel

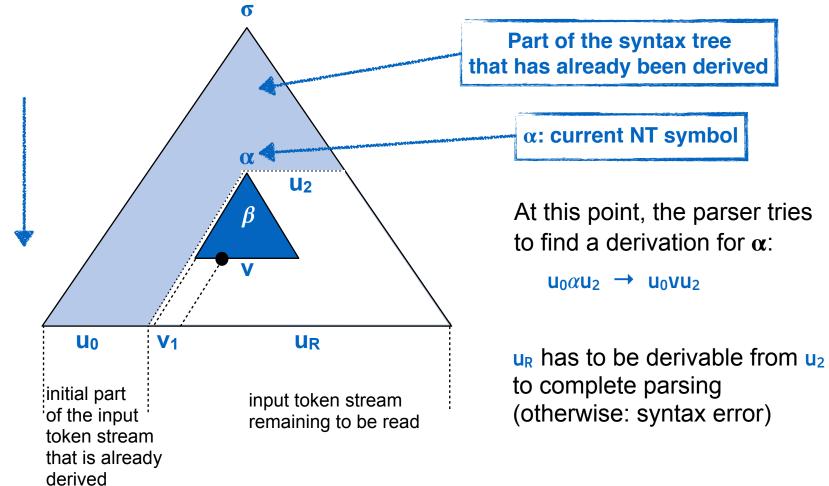
#### Overview

- Bottom-up parsing revisited
- Deciding when to reduce
- LR parsers
  - General idea
  - LR(1) parsers
  - LALR



#### **Top-down parsing**

LL(1) parsers generate a parse tree from top to bottom:

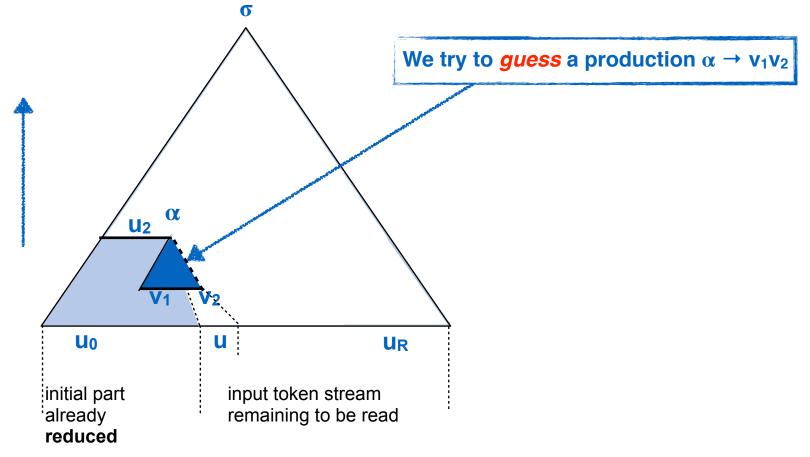




#### **Bottom-up parsing**



Can we also construct the parse tree from bottom to top?

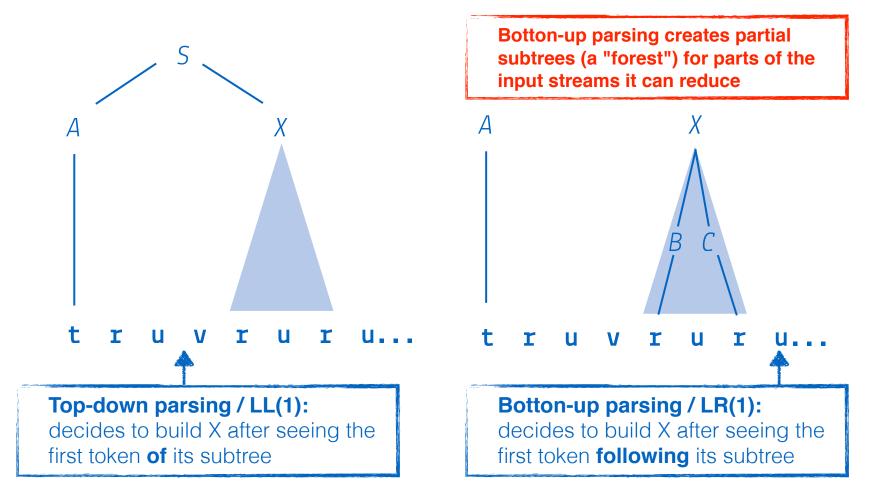




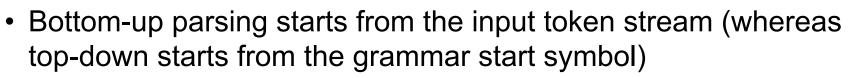
## Parsing compared in detail



Top-down and bottom-up parsing and syntax tree construction



## General idea of bottom-up parsing



- It *reduces* a string to the start symbol by *inverting productions* 
  - trying to find a production matching the *right hand side*

$$E \rightarrow T + E \mid T$$
  
$$T \rightarrow int \times T \mid int \mid E$$

- Consider the input token stream int \* int + int:
- Reading the productions in reverse (from *bottom* to *top*) gives a *rightmost derivation*

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$$E \leftarrow T + E \mid T$$

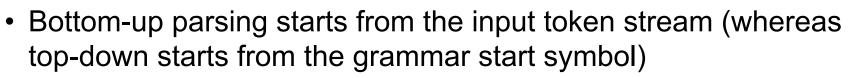
$$T \leftarrow int \times T \mid int \mid E$$

int 
$$\times$$
 int  $+$  int $T \rightarrow$  intint  $\times$   $T$   $+$  int $T \rightarrow$  int  $\times$   $T$  $T$   $+$  int $T \rightarrow$  int $T$   $+$   $T$  $E \rightarrow$   $T$  $T$   $+$   $E$  $E \rightarrow$   $T + E$  $E$ 

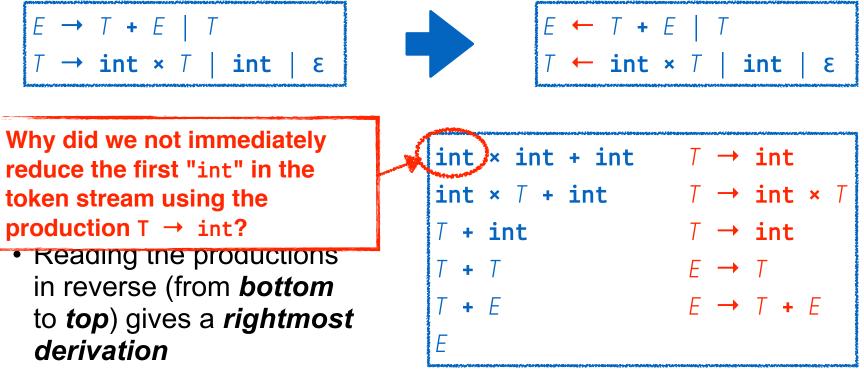
Syntax

analvsis

## General idea of bottom-up parsing



- It *reduces* a string to the start symbol by *inverting productions* 
  - trying to find a production matching the *right hand side*





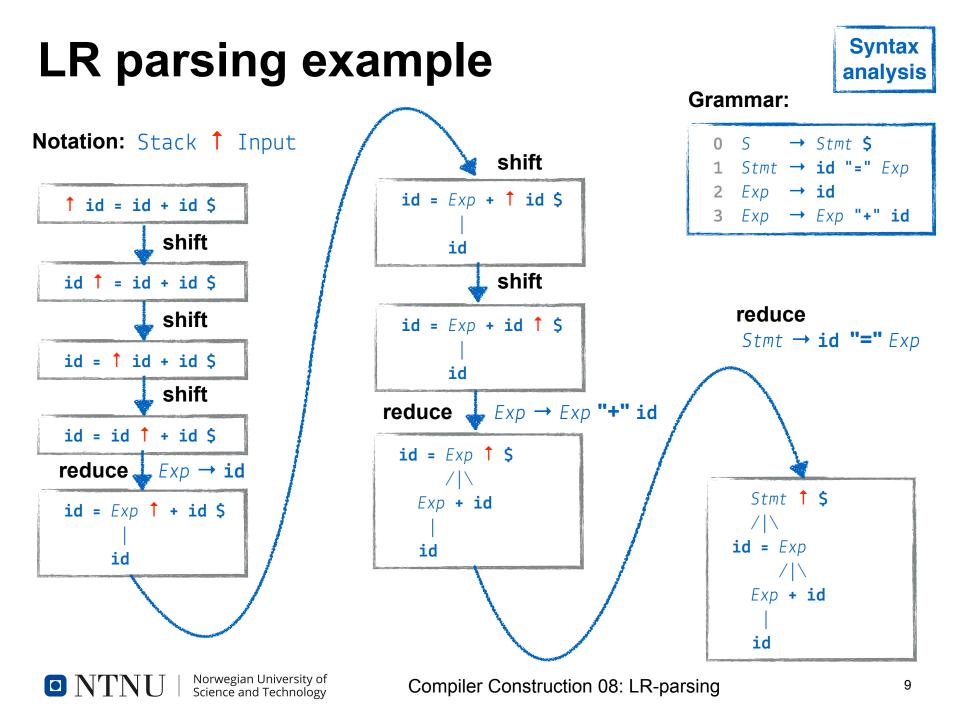
**Syntax** 

## Taking right decisions: LR parsing



**Idea:** we extend the general idea of bottom-up parsing:

- Add the EOF token (\$) and an extra start rule
  - This helps to uniquely identify when we constructed the root node of the parse tree
- As before, the parser uses a stack of terminal and NT symbols
- The parser looks at the current input token and decides between one of the following actions:
  - shift: Push the input token onto the stack, read the next token
  - reduce: Match the top symbols on the stack with a production righthand side. Pop those symbols and push the left-hand side nonterminal. At the same time, build this part of the tree
  - **accept**: when the parser is about to shift \$, the parse is complete
- The parser uses a DFA (encoded in a table) to decide which action to take and which state to go to after each shift action



# LR(1) items

LR(1)

- Syntax analysis
- The parser uses a DFA (a deterministic finite automaton) to decide whether to shift or reduce
  - The states in the DFA are sets of LR items

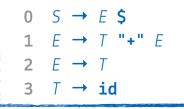
item: 
$$\chi \rightarrow \alpha \bullet \beta$$
 t,s

- An LR(1) item is a production extended with:
  - A dot (•), corresponding to the position in the input sentence
  - One or more possible lookahead terminal symbols, t,s (we will use ? when the lookahead doesn't matter)
- The LR(1) item corresponds to a state where:
  - The topmost part of the stack is  $\boldsymbol{\alpha}$
  - The first part of the remaining input is expected to match  $\beta(t|s)$

## Parser DFA: constructing state 1

First, take the start production and place the dot in the beginning...





**Syntax** 

analysis

 $S \rightarrow \bullet E \mathbf{\dot{S}}$ ?  $S \rightarrow \bullet E \mathbf{\dot{S}}$ • T "+" F \$ state 1  $S \rightarrow \bullet F S$ ? \$ • T "+" F \$ +,\$  $T \rightarrow \bullet id$ 

Note that there is a nonterminal

*E* right after the dot, and it is followed by a terminal \$. Add the productions for *E*, with \$ as the lookahead

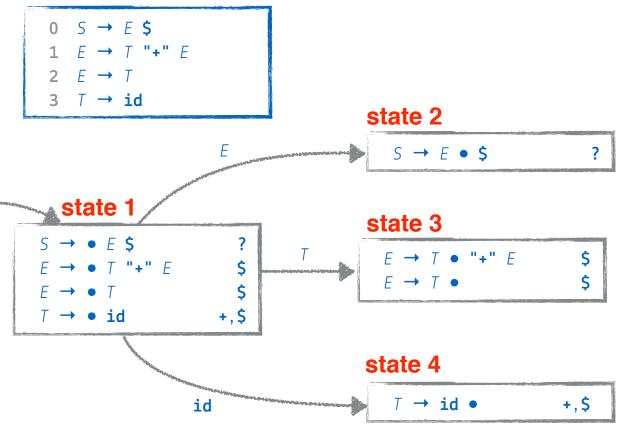
There is a nonterminal T right after the dot, and which is followed by either "+" or \$. Add the productions for T, with "+" and \$ as the lookahead. (We write them on the same line as a shorthand.)

We have already added productions for all NTs that are right after the dot. Nothing more can be added. We are finished constructing **state 1** 

Adding new productions for nonterminals following the dot, until no more productions can be added, is called **taking the closure** of the LR item set



#### **Constructing the next states**

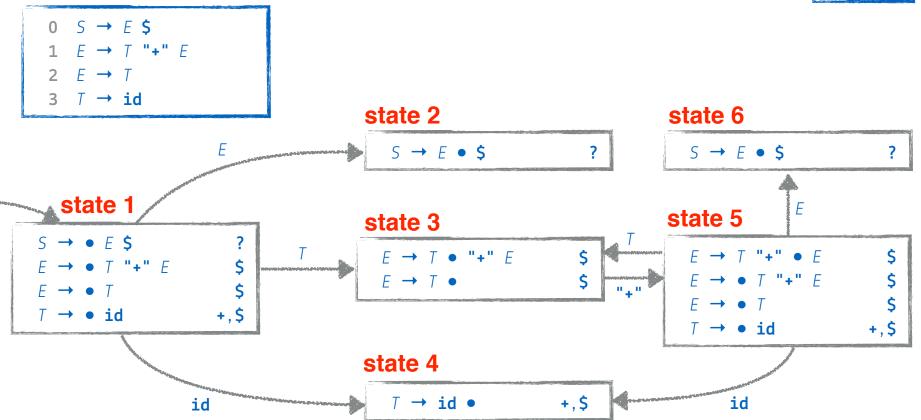


Note that the dot is followed by *E*, *T*, and **id** in state 1.

For each of these symbols, create a new set of LR items, by advancing the dot passt that symbol. Then complete the states by taking the closure (Nothing had to be added for these states.)

**Syntax** 

#### **Completing the LR DFA**



Complete the DFA by advancing the dot, creating new states, completing them by taking the closure.

If there is already a state with the same items, we use that state instead.

**Syntax** 

## **Constructing the LR table**



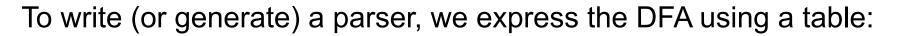
- For each token edge t, from state j to state k, add a shift action "s k" (shift and goto state k) to table[j,t]
  - = reading a token and pushing it onto the stack
- For each state j that contains an LR item where the dot is at the end, add a reduce action "r p" (reduce p) to table[j,t], where p is the production and t is the lookahead token
  - = popping the right-hand side of a production off the stack
- For each nonterminal edge X, from state j to state k, add a goto action
   "g k" (goto state k) to table[j,X]
  - = pushing the left-hand side nonterminal onto the stack

state	"+"	id	\$ E	Т
1				
2				
3				
4				
5				
6				

- For a state j containing an LR item with the dot to the left of \$, add an accept action "a" to table[j,\$].
  - If we are about to shift \$, the parse has succeeded

**Synta** 

## **Constructing the LR table**



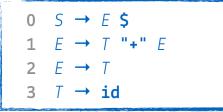
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state	"+"	id	\$	Е	Т
1		s <b>4</b>		g <mark>2</mark>	g <mark>3</mark>
2			а		
3	s <mark>5</mark>		r p2		
4	r p3		r p3		
5		s <mark>4</mark>		g <mark>6</mark>	g <mark>3</mark>
6			r p1		

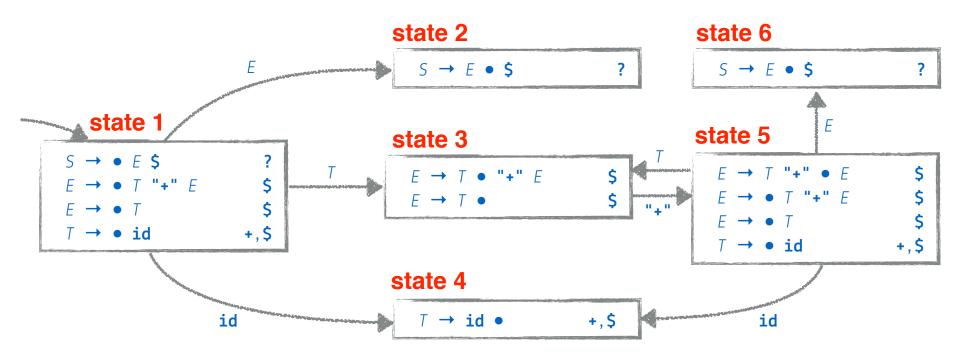
- For a state j containing an LR item with the dot to the left of \$, add an accept action "a" to table[j,\$].
  - If we are about to shift \$, the parse has succeeded

**Synta** 





state	"+"	id	\$	Е	Т
1		s 4		g <mark>2</mark>	g <mark>3</mark>
2			а		
3	s <mark>5</mark>		r p2		
4	r p3		r p3		
5		s <mark>4</mark>		g <mark>6</mark>	g <mark>3</mark>
6			r p1		





## LR parsing algorithm

```
push $;
push start state, s0;
word ← NextWord();
while (true) {
    state ← top of stack;
    if Action[state,word] = "reduce \mathbf{A} \rightarrow \mathbf{\beta}" {
         pop 2 × |\beta| symbols; // 2 × |\beta| due to terminal symbol and state
         state ← top of stack;
         push A;
         push Goto[state, A];
    }
    else if Action[state,word] = 'shift s<sub>i</sub>' {
         push word;
         push s<sub>i</sub>;
         word ← NextWord();
    }
    else if Action[state,word] = "accept" { break; }
    else Fail();
}
return success; /* executed break on 'accept' case */
```

**Syntax** 

## Using the LR table for parsing

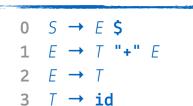
- Use a symbol stack and a state stack
  - · The current state is the state stack top
- Push state 1 to the state stack
- Perform an action for each token:
- Case Shift s:
  - Push the token to the symbol stack
  - Push s to the state stack
  - · The current state is now s
- Case Reduce p:
  - Pop symbols for the RHS of p
  - Push the LHS symbol X of p
  - Pop the same number of states
  - Let s1 = the top of the state stack
  - Let s2 = table[s1,X]
  - Push s2 to the state stack
  - The current state is now s2
- Case Accept: Report successful parse

state	"+"	id	\$	E	Т
1		s <b>4</b>		g <mark>2</mark>	g <mark>3</mark>
2			а		
3	s <mark>5</mark>		r p2		
4	r p3		r p3		
5		s <mark>4</mark>		g <mark>6</mark>	g <mark>3</mark>
6			r p1		



**Syntax** 

#### LR parsing example



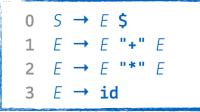
state	"+"	id	\$	E	Т
1		s <mark>4</mark>		g <mark>2</mark>	g <mark>3</mark>
2			а		
3	s <mark>5</mark>		r p2		
4	r p3		r p3		
5		s <mark>4</mark>		g <mark>6</mark>	g <mark>3</mark>
6			r p1		
			-		

Parsing id "+" id \$

state stack	symbol stack	input	action
1		id "+" id \$	shift 4
14	id	"+" id \$	reduce p3
13	Т	"+" id \$	shift <mark>5</mark>
135	T "+"	id \$	shift <mark>4</mark>
1354	7 <b>"+" id</b>	\$	reduce p3
1353	T "+" T	\$	reduce p2
1356	T "+" E	\$	reduce p1
12	E	\$	accept

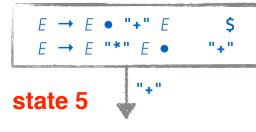
**Syntax** 

#### **Conflict in an LR table**



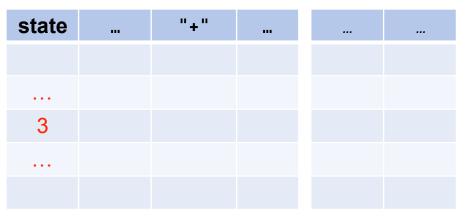
Parts of the DFA:

#### state 3



#### Different grammar to previous example!

Parts of the parse table:



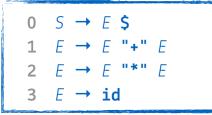
Fill in the parse table – what is the problem?



**Syntax** 

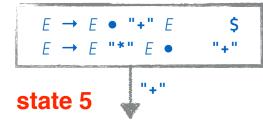
#### **Conflict in an LR table**





Parts of the DFA:

#### state 3



Parts of the parse table:

state	 "+"	 	
3	s <mark>5</mark> , r p2		

There is a shift-reduce conflict, the grammar is ambiguous. In this case, we can resolve the conflict by selecting one of the actions.

To understand which one, think about what the top of the stack looks like. Think about what will happen later if we take the shift rule or the reduce rule.

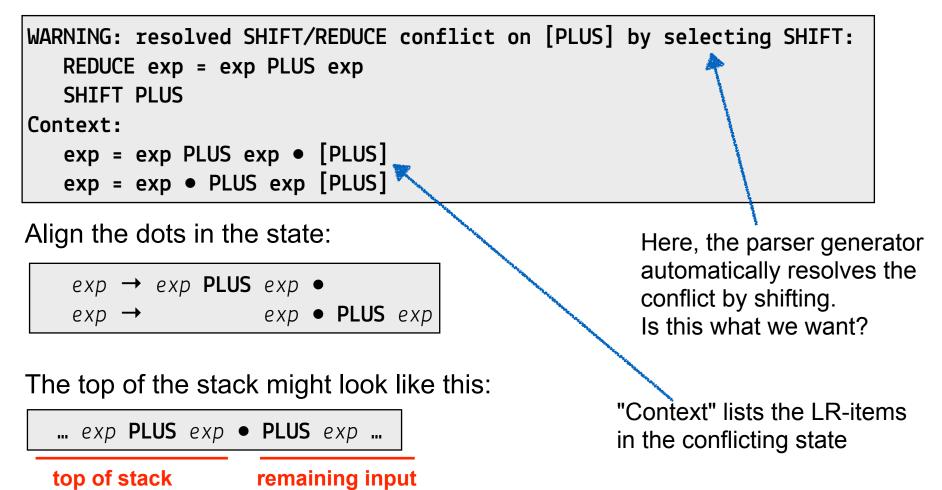
## Analyzing LR conflicts

Example parser generator output:

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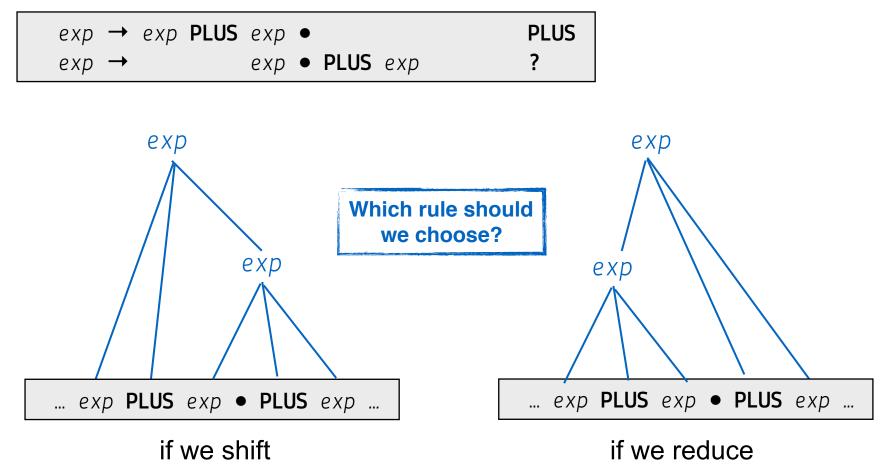


**Syntax** 

## Analyzing LR conflicts



Align the dots in the state:

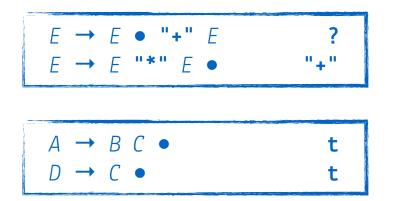




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#### **Different kinds of conflicts**





a **shift-reduce** conflict

a **reduce-reduce** conflict

Shift-reduce conflicts can sometimes be solved with precedence rules. In particular for binary expressions with priority and associativity.

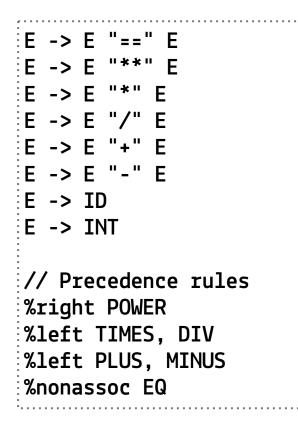
For other cases, you need to carefully analyze the shift-reduce conflicts to see if precedence rules are applicable, or if you need to change the grammar.

For reduce-reduce conflicts, it is advisable to think through the problems, and change the grammar.



## **Typical precedence rules**

Precedence rules for an LR expression grammar might look like this:



Shift-reduce conflicts can be automatically resolved using *precedence rules* 

Operators in the same rule have the same priority

• e.g., PLUS, MINUS

Operators in an earlier rule have higher priority

 e.g. TIMES has higher priority than PLUS)

## How the precedence rules work

A rule is given the priority and associativity of its rightmost token For two conflicting rules with different priority, the rule with the highest priority is chosen:



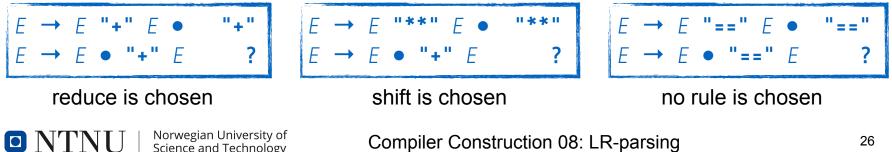
reduce is chosen



shift is chosen

Two conflicting rules with the same priority have the same associativity

- Left-associativity favors reduce, right-associativity favors shift
- Non-associativity removes both rules from the table
  - input following that pattern will cause a parse error



**Syntax** 

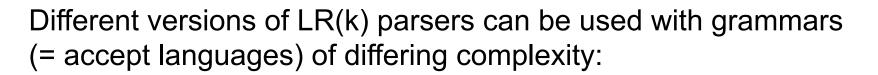
## **Different variants of LR(k) parsers**

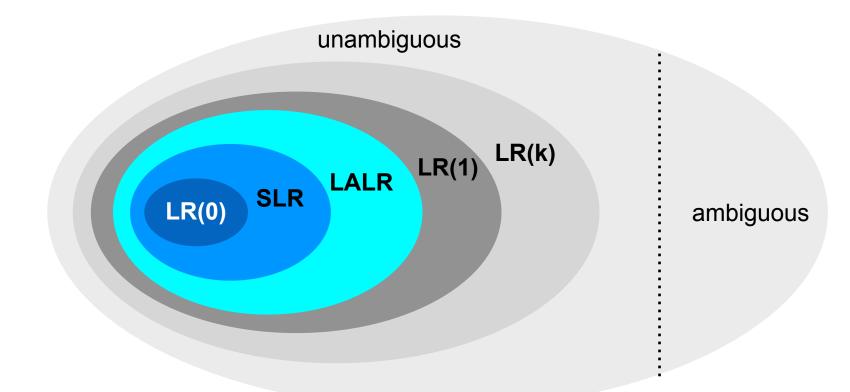


Туре	Characteristics
LR(0)	LR items without lookahead Not very useful in practice.
SLR Simple LR	Look at the FOLLOW set to decide where to put reduce actions Can parse some useful grammars
LALR(1)	Merges states that have the same LR items, but different lookaheads (LA) $\rightarrow$ leads to much smaller tables than LR(1)
often used in practice	Used by most well known tools: yacc, CUP, Beaver, SableCC, Sufficient for most practical parsing problems
LR(1)	Slightly more powerful than LALR(1) Not used in practice – the tables become very large
LR(k)	Far too large tables for k>1



## Different variants of LR(k) parsers





All context-free (type 2) grammars



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**Syntax** 

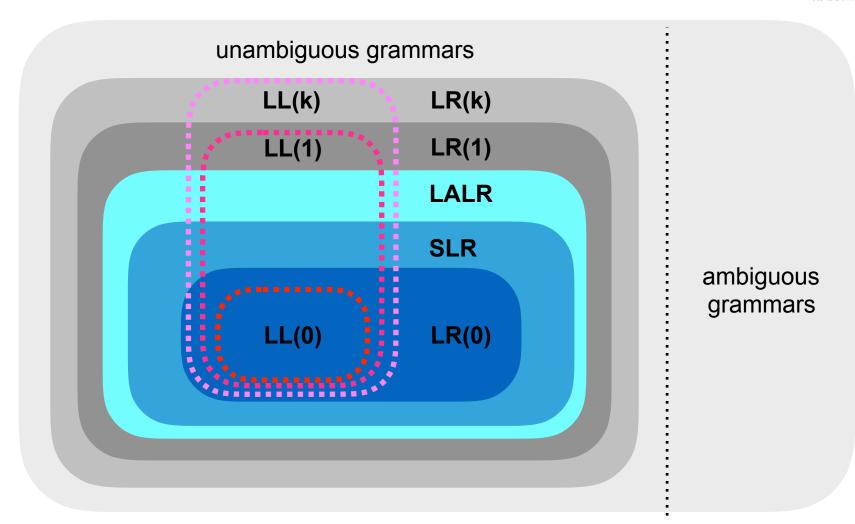
## LL(k) vs LR(k) parsers



	LL(k)	LR(k)	
Parses input	Left-to-right		
Derivation	Leftmost	<b>R</b> ightmost	
Lookahead	<b>k</b> s	symbols	
Build the tree	top down	bottom up	
Select rule	after seeing titshe first k tokens	after seeing all of its tokens plus additional tokens	
Left recursion	no	yes	
Unlimited common prefix	no	yes	
Resolve ambiguities through rule priority	dangling else	dangling else, associativity, priority	
Error recovery	trial-and-error	good algorithms exist	
Implement by hand?	possible	too complicated use a generator	



## LL(k) vs. LR(k) grammars



**Syntax** 

#### What's next?

Syntax analysis

- Practical considerations when constructing parsers
- Overview of Parser generators
- Using the yacc parser generator and examples
  - Interaction between yacc and lex

